

Angular Distribution of Gray Particles in High Energy $\nu\mu$ - Ne Interaction

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$\nu\mu$ - Ne

(-)

$\langle \cos\theta \rangle$ $\langle \theta \rangle$

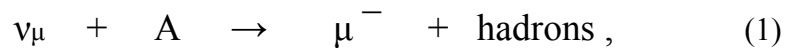
400 MeV) $\leq E \leq$ The angular distribution of the gray particles (protons in the energy range 30 emitted in the interaction of high energy hadrons with nuclei are investigated here. Gray particles'g particles' are assumed to result from the intranuclear cascade initiated by the passage of the incident hadron through the nucleus. We focus our study on the case where the cascade results from a single collision suffered by the projectile. Such reaction, which are free from higher successive projectile target nucleon collisions, are believed to occur in high energy neutrino-nucleus interaction. The proposed model is formulated in the frame work of Glauber approximation. It is found that the grey is particles arise only from the first two generations of the cascade, their angular distribution calculated here. The $\langle \theta \rangle$ and $\langle \cos\theta \rangle$ are found to agree satisfactorily with available experimental data.

Key words : Angular distribution, Glauber intranuclear cascade, gray particles, GN1, GN2.

INTRODUCTION

Over the past few years interest has been growing in high energy hadron nucleus (hA) interaction and a vast amount of experimental data has already been accumulated. The reason is that, the mechanism of the particle production in nuclei is still in much debate (Tosson *et al.* 1994). Many theoretical models picture the hA interaction as a sequence of independent hA collisions inside the nucleus. Thus the number of collisions, ν , encountered by the incident hadron is used in these models as a basic parameter to describe the particle production on nuclei. The commonly known approach is to deduce ν from the number of produced "gray particles" N_g . These are mainly recoil target protons in the momentum range $0.2 \div 1$ GeV/c (energy range $30 \leq E \leq 400$ MeV). Their angular distribution peaks in the forward direction, and they are emitted during or shortly time after the passage of the leading hadron. They are therefore close to the primary sequence (pre-equilibrium stage) of the interaction and thus reflected to bear important information about the interaction mechanism. To be more specific if the N_g distribution for a single collision ($\nu=1$) is known, then the distribution for any other ν value can be constructed in an incoherent manner. Moreover, the final state hadronic system in the single collision will reflect only the inter-nuclear cascade and thereby eases the interpretation of the process.

In this paper the charge current neutrino-nucleus ($\nu_\mu A$) interaction is focused, e.g.



and the intranuclear cascade model is developed to calculate the angular distribution of g particles. In the following the description of the proposed model formulated in the frame work of Glauber approximation (Glauber 1959) is presented. Results of calculations and comparison with the experimental data as well as previous theoretical approaches are clarified.

MODEL AND FORMULATION

The subsequent intranuclear cascade of $\nu_\mu A$ interaction can be pictured as follows :

- (i) The incident high energy neutrino approaches the target nucleus at an impact parameter \bar{b} . As it passes through the nucleus, it may interact with a nucleon and disappears. The resulting muon does not reinteract in the nucleus (Griffiths 1987). The final state will thus reflect the intranuclear cascade. In such a reaction, neutrino interacts with a quark in a target nucleon via weak interaction basis. The resulting quark, considered as a leading particle system (LPS) may rescatter in the nucleus as a single quark before it disintegrates into a meson. This LPS is estimated to have a negligible effect on the Ng production (Enaiah 2000). We are thus left with the struck nucleon which recoils inside the nucleus. This nucleon constitutes the primary of the first generation "GN1". It has a 50% chance to pass the velocity window $0.3 < \beta < 0.7$ for gray particles. It is, therefore, rather fast and travels mostly in the forward direction. We shall assume for simplicity that they travel along the same impact parameter \bar{b} as the projectile.
- (ii) The primary nucleon rescatters with other nucleons yielding the second generation "GN2". All protons from this generation are counted as gray particles. Pions from the decay of the probably excited primary nucleon are usually too slow to produce gray particles in a meson-nucleon collision.
- (ii) The secondaries collide with other target nucleons to produce the third generation and so until a compound nucleus is formed and decay from energy degradation estimates (Hufner 1987). It can be shown that the third and higher order generations contribute only to the black particles ($\beta < 0.3$) resulting from the final stage of the reaction (evaporation of the final nucleus). They are therefore also left out.

The visualization of the $\nu_{\mu}A$ interaction is represented schematically in Fig (1).

The above model can be formulated mathematically for $\nu_{\mu}A$ interaction as follows: The projectile neutrino characterized by the trajectory $\bar{r} = (\bar{b}, z)$ interacts with a target nucleon at z_1 , ($-\infty < z_1 < \infty$) and vanishes. The probability that this nucleon will emerge as a gray proton will be noted as P_{γ} . It is just the product of the probability P_p that it will recoil as a proton and the probability P_g (~ 0.5) that it will be gray (Enaiah 2000).

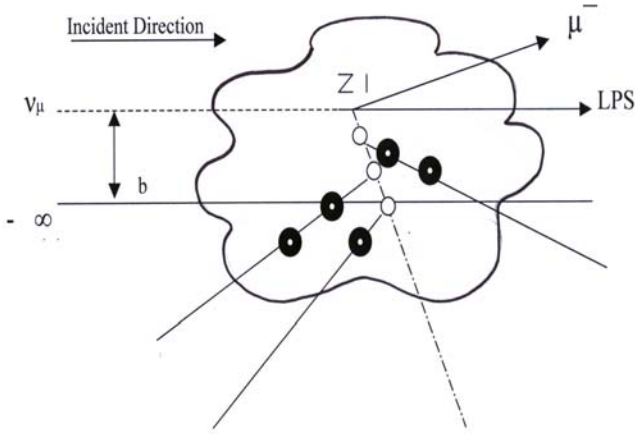


Fig.1 : The intranuclear cascade initiated by a very high energy neutrino. The incident neutrino strikes at Z1 . The recoiling primary nucleon(-----)collide with secondary nucleons (O) . Tertiary collisions are denoted by (●) .

$$P_\gamma = P_p P_g \tag{2}$$

To determine P_p one should notice that the final state nucleon is a proton in 50% of charge-current interactions with a neutrino and in 100 % of the interaction with a proton ,i.e

$$P_p = \frac{q\sigma_{\nu p} + 0.5(1-q)\sigma_m}{\sigma_{\nu p} + \sigma_m} \tag{3}$$

which gives $P_p = 1/3$ for $q = \text{charge } Z/A$,i.e. for $Z = A/2$ nuclei (light nuclei) . Thus the number of the gray proton, n , from GN1 is either zero or one. The primary nucleon rescatters from N_1 target nucleons GN2 of

which N_2 are gray protons. The number of gray particles from this event is therefore

$$N_g = n + N_2 \tag{4}$$

The probability for this event is

$$I(\bar{b}, N_1, n, N_2) = \int e^{-\sigma \nu T(-\infty, z_1)} \frac{dz_1}{\lambda_\nu} Q^{1(n)} I_{N_1, N_2}(\bar{b}, z_1) \tag{5}$$

The first factor, under the integration sign ,represents the probability for no projectile interaction uptill z_1 . The second factor namely dz_1/λ_ν is the probability that the neutrino nucleon interaction takes place between z_1 and z_1+dz .The main-free-path of λ_ν at the point (\bar{b}, z) is given by

$$\frac{1}{\lambda} = \sigma \nu \rho(\bar{r}) \tag{6}$$

where $\rho(\bar{r})$ is the target nuclear density normalized to the mass number A, and nuclear thickness

$$\begin{aligned} T(\bar{b}) &= T(-\infty, z_1) + T(z_1, \infty) \\ &= \int_{-\infty}^{\infty} dz/d\lambda \end{aligned} \quad (7)$$

The third factor, $Q_{1(n)}$, is the probability of whether the struck nucleon will recoil as a gray proton or not ($n=0,1$).

The final factor, gives the probability that the recoiling struck nucleon travelling from z_1 to ∞ (with impact parameter \bar{b}) will collide N_1 times, out of which N_2 are gray protons (Enaiah 2000, Tosson *et al.* 1994), i.e.,

$$I_{N_1, N_2}(\bar{b}, z_1) = \left\{ \left(\frac{[\sigma T(z_1, \infty)]^{N_1}}{N_1!} \right) e^{-\sigma T(z_1, \infty)} \right\} \left\{ \binom{N_1}{N_2} q^{N_2} (1-q)^{(N_1-N_2)} \right\} \quad (8)$$

where σ is considered as an effective cross-section which was found from fitting the experimental $\langle N_g \rangle$ values in high-energy hA interaction (Tosson *et al.* 1994)

$$\sigma = 30 \pm 3 \text{ mb} \quad (9)$$

The probability for N_g gray particles to be observed in the interaction along an impact parameter \bar{b} is thus :

$$H(N_g, \bar{b}) = \sum_{N_1, n, N_2} \delta(N_g - n - N_2) I(\bar{b}, n, N_1, N_2) \quad (10)$$

Carrying out the summation over N_1 and N_2 one gets

$$H(N_g, \bar{b}) = \sum_{n=0,1}^{Min(N_g, 1)} Q(n) \int \exp[-\sigma_v T(-\infty, Z_1)] \frac{dz_1}{\lambda_v} \frac{(q\sigma T(z_1, \infty))^{N_g - n_o}}{(N_g - n_o)!} \exp[-q\sigma T(z_1, \infty)]$$

(11)

As mention above $\sum_{n=0,1}^{Min(N_g,1)} Q(n)$ will equal 1. Now let ,

$$N_g - n_o = \mu$$

equation (11) will take a form

$$H(N_g, \bar{b}) = \int e^{-\sigma T(-\infty, z_1)} \frac{dz_1}{\lambda_\nu} \frac{[\sigma_N T(z_1, \infty)]^\mu}{\mu!} e^{-\sigma_N T(z_1, \infty)} \quad (12)$$

The partial cross section (geometrical factor) for primary struck nucleon to suffer μ secondary collisions for the single neutrino interaction G_μ is given by

$$G_\mu = \int d^2 b H(N_g, \bar{b}) \quad (13)$$

Similary the geometrical factor $G_{\mu\eta}$ represents the partial cross section for μ th secondary to suffer η tertiary collisions is given by

$$G_{\mu\eta} = \mu I_\eta G_\mu \quad (14)$$

where,

$$I_\eta \cong \frac{[0.5\sigma T(b=0)]^\eta}{\eta!} e^{-\frac{1}{2}\sigma T(b=0)} \quad (15)$$

The inclusive cross-section for the production of gray particl “g” of momentum \bar{p} in the V_μ A reaction may be decomposed in to the sum

$$\frac{d^3\sigma}{d\bar{p}^3} = p_p \sum_\mu G_\mu D(\bar{p}) + \sum_\mu \sum_\eta G_{\mu\eta} D_{\mu\eta}(\bar{p}) \quad (16)$$

where D_μ ($D_{\mu\eta}$) gives the corresponding dynamical factor in the first(second) generation. The former is taken to be a Poisson like form, while the latter is taken to Gaussian as in Ref. (Hufner & Knoll 1977) (see the Appendix).

$$R(\bar{p}) = \frac{1}{(2\pi)^{\frac{3}{2}}} \frac{1}{\langle \sigma_{11}^2 \rangle^{\frac{1}{2}}} \frac{1}{\langle \sigma_{\perp}^2 \rangle} \exp\left(-\frac{(p_{11} - \langle p_{11}^2 \rangle)}{2\langle \sigma_{11}^2 \rangle} - \frac{p_{\perp}^2}{2\langle \sigma_{\perp}^2 \rangle}\right)$$

where

$$p_{11} = p \cos(\theta) \quad , \quad p_{\perp} = p \sin(\theta) \quad (17)$$

When this equation is integrated over the momentum values, gives the angular distribution. i.e,

$$\begin{aligned} \frac{d\sigma}{d\Omega} &= \frac{1}{2} \frac{d\sigma}{d(\cos\theta)} \\ &= \sum_{\mu} G_{\mu} \int_0^{\infty} R_{\mu}(\bar{p}) p^2 dp + \sum_{\mu} \sum_{\eta} \mu I_{\eta} G_{\mu} \int_0^{\infty} R_{\mu\eta}(\bar{p}) p^2 dp \\ &= \sum_{\mu} G_{\mu} [R(\theta) + \mu \sum_{\eta} I_{\eta} R_{\mu\eta}(\theta)] \end{aligned} \quad (18)$$

where,

$$R(\theta) = \int_0^{\infty} R_{\mu\eta}(\bar{p}) p^2 dp$$

In the integration over momentum values, care should be taken that momentum ranges $0.2 \div 1$ GeV/c (energy range $30 \leq E \leq 400$ Mev).

COMPARISON WITH EXPERIMENT

The calculations for the angular distribution of g particles produced in $\nu\mu A$ reaction is shown in Fig. (2), (notice that the angular distribution is practically dominated by secondaries). This Fig. represents a comparison of the present calculation with those of the Monte Carlo cluster model (Bogatskaya *et al.* 1977).

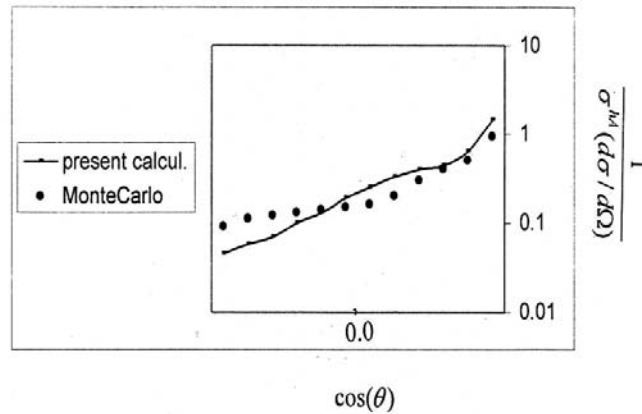


Fig. 2 : Angular distribution of g particles in ν_{μ} -Ne interaction. Data taken from Ref.[3].

On the whole, the present approach gives the best obtained agreement (in the shape and magnitude) with the experiment (Bogdanowicz *et al.* 1963). I consider this agreement is an additional justification that g particles are only produced from the first and second generation and mostly second generation. Table 1 summarizes the present calculation of the mean emission angle $\langle\theta\rangle$ and $\langle\cos\theta\rangle$ for the g particles from GN1 and GN2 with the corresponding experimental average values.

Table 1. The present calculation with corresponding experimental values

	Present calculation	Experiment
$\langle\theta\rangle$ (total) (GN2)	58.5° 76.5°	$67 \pm 2^\circ$
$\langle\cos\theta\rangle$ (total) (GN2)	0.44 0.20	0.32 ± 0.01

Appendix The Dynamic Factors D_{μ} And $D_{\mu\eta}$

Guided by the Gluber result (Hufner & Knoll 1977), the factor $D_{\mu}(\mathbf{p})$ and $D_{\mu\eta}(\mathbf{p})$ describing the momentum distributions for GN1 and GN2 are taken to be Gaussian,

$$D_i(\vec{p}) = \left[(2\pi)^{3/2} \langle \sigma_{\parallel}^2 \rangle_i^{1/2} \langle \sigma_{\perp}^2 \rangle_i \right]^{-1} \exp \left[-\frac{(\mathbf{p}_{\parallel} - \langle \mathbf{p}_{\parallel} \rangle_i)^2}{2 \langle \sigma_{\parallel}^2 \rangle_i} - \frac{\mathbf{p}_{\perp}^2}{2 \langle \sigma_{\perp}^2 \rangle_i} \right] \quad (\text{A-1})$$

Where the subscript i stands for either μ or $\mu\eta$. The mean momenta for the first and second generations satisfy,

$$\langle \mathbf{P}_{\parallel} \rangle_{\mu} = (1 - \phi_1)^{\mu} \langle \mathbf{P}_{\parallel} \rangle_0$$

$$\langle \mathbf{P}_{\parallel} \rangle_{\mu\eta} = (1 - \phi_2)^{\eta} \langle \mathbf{P}_{\parallel} \rangle_{\mu_0} \quad (\text{A-2})$$

2)

where,

$$\langle \mathbf{P}_{\parallel} \rangle_{\mu_0} = \phi_1 (1 - \phi_1)^{\mu-1} \langle \mathbf{P}_{\parallel} \rangle_0 \quad (\text{A-3})$$

The parameter $\phi_1(\phi_2)$ is the fraction of momentum lost by the primary (secondary) recoiling nucleon in a collision with a secondary (tertiary) nucleon. The recursion relations for the widths are rather more complicated,

$$\begin{aligned} \langle \sigma_{\parallel}^2 \rangle_{\mu} &= (1 - \phi_1 - \beta_1) \langle \sigma_{\parallel}^2 \rangle_{\mu-1} + (\phi_1 - \beta_1) (\mathbf{k}_F^2/5) \\ &+ \beta_1 [\langle \sigma_{\perp}^2 \rangle_{\mu-1} + (\mathbf{k}_F^2/5)] \\ &+ (\phi_1 - \phi_1^2 - \beta_1) \langle \mathbf{P}_{\parallel} \rangle_{\mu-1}^2 \end{aligned} \quad (\text{A-4a})$$

$$\begin{aligned} \langle \sigma_{\perp}^2 \rangle_{\mu} &= (1 - \phi_1 - (\beta_1/2)) \langle \sigma_{\perp}^2 \rangle_{\mu-1} + (\mathbf{k}_F^2/5) (\phi_1 - (\beta_1/2)) \\ &+ (\beta_1/2) [\langle \sigma_{\parallel}^2 \rangle_{\mu-1} + (\mathbf{k}_F^2/5) + \langle \mathbf{P}_{\parallel} \rangle_{\mu-1}^2] \end{aligned} \quad (\text{A-4b})$$

$$\begin{aligned} \langle \sigma_{\parallel}^2 \rangle_{\mu\eta} &= (1 - \phi_2 - (\beta_2)) \langle \sigma_{\parallel}^2 \rangle_{\mu,\eta-1} + (\mathbf{k}_F^2/5) (\phi_2 - \beta_2) \\ &+ (\beta_2) [\langle \sigma_{\perp}^2 \rangle_{\mu,\eta-1} + (\mathbf{k}_F^2/5)] \\ &+ (\phi_2 - \phi_2^2 - \beta_2) \langle \mathbf{P}_{\parallel} \rangle_{\mu,\eta-1}^2 \end{aligned} \quad (\text{A-4c})$$

$$\begin{aligned}
\langle \sigma_{\perp}^2 \rangle_{\mu\eta} &= (1 - \phi_2 - (\beta_2/2)) \langle \sigma_{\parallel}^2 \rangle_{\mu, \eta-1} \\
&+ (k_F^2/5) (\phi_2 - \beta_2/2) + (\beta_2/2) [\langle \sigma_{\parallel}^2 \rangle_{\mu, \eta-1} \\
&+ (k_F^2/5) + \langle P_{\parallel} \rangle_{\mu, \eta-1}^2]
\end{aligned} \tag{A-4d}$$

where k_F is the Fermi momentum (~ 260 MeV).

The initial values for Eqs. (A-2 and A-4) are,

$$\begin{aligned}
\langle P_{\parallel} \rangle_o &\cong 0.5 \div \text{GeV}/c, \quad \langle \sigma_{\parallel}^2 \rangle_o = k_F^2/5, \\
\langle \sigma_{\perp}^2 \rangle_o &\cong 0.08 (\text{GeV}/c)^2
\end{aligned} \tag{A-5}$$

and,

$$\begin{aligned}
\langle \sigma_{\parallel}^2 \rangle_{\mu o} &= (k_F^2/5) (1 - \phi_2 - \beta_1) (\phi_1 - \beta_1) \langle \sigma_{\parallel}^2 \rangle_{\mu, \eta-1} \\
&+ \beta_1 [\langle \sigma_{\perp}^2 \rangle_{\mu-1} + (k_F^2/5)] \\
&+ (\phi_2 - \phi_1^2 - \beta_2) \langle P_{\parallel} \rangle_{\mu-1}^2
\end{aligned} \tag{A-6}$$

$$\begin{aligned}
\langle \sigma_{\perp}^2 \rangle_{\mu o} &= (k_F^2/5) (1 - \phi_1 - (\beta_1/2)) + (\phi_1 - (\beta_1/2)) \langle \sigma_{\perp}^2 \rangle_{\mu-1} \\
&+ (\beta_2/2) [\langle \sigma_{\parallel}^2 \rangle_{\mu-1} + (k_F^2/5) + \left\langle P_{\parallel} \right\rangle_{\mu-1}^2]
\end{aligned} \tag{A-7}$$

In our calculations we have taken,

$$\phi_1 = \phi_2 = 0.25 \quad \text{and} \quad \beta_1 = \beta_2 = (2\phi/3). \tag{A-8}$$

REFERENCES

Anderss, B., Gorpman, S. I. A. & Nilsson, G. 1983. Monte Carlo simulation for $v=1$, Nuclear Physics B191: 173 - 180.

- Bogatskaya, N. G., Elieev, S. M., Zinovev, G. M. & Sov, J. 1977.** Monte Carlo cluster model. *Nuclear Physics* 26: 535.
- Bogddanowicz, J., Ciok, P., Saniewska, T. & Zielinski, P. 1963.** Some feature of the interaction of 24 GeV proton with heavy nuclei in emulsion, *Nuclear Physics* 40: 270-281.
- Enaiah, N. A. 2000.** Study of semi-classical approximation in quantum, Ph.D Thesis Riyadh, King Saud University.
- Glauber, R. J. 1959.** Lectures in Theoretical Physics. Vol. I, (Edited by Brittan, W. E. & Dunham, L. G.), pp. 315- 414. Interscience, New York.
- Griffiths, D. 1987.** Introduction to elementary particles, Johnwiley and Saus. New York.
- Hufner, J. 1987.** Hadronic processes inside nuclei, *Nuclear Physics* A352.
- Hufner, J. & Knoll, J. 1977.** Rows and rows atheory for collisions between heavy ions at high energy, *Nuclear Physics* A290: 460 - 468.
- Tosson, M., Osman, M. O., Osman, M. M & Hegab, M. K. 1994.** Study of fast target protons in high energy hadron-nucleus collisionns, *Zeitschrift Für Physika* A347: 247-253.
- Suzuki, N. 1983.** The distribution of gray particles in lepton induced reactions, *Nuclear Physics* A403: 553 - 562.

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